Evaluation

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It varies. It doesn't hurt to quote it

The symbol NIL is often pre-set with the value ()

Or sometimes the symbol ${\tt nil}$. Sometimes case of symbols is important, sometimes not

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In Common Lisp they are the same symbol

Even stranger, in Common Lisp () is considered *syntactically* identical to NIL, so () is classed as a symbol as well as a list

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This is not self-evaluation: just that the value is itself!

Exercise: what would happen if you set the value of t to ()?

Other Lisps have a separate Truth datatype for true and false

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Other Lisps have a separate Truth datatype for true and false

So () is invalid in a Boolean expression

Still others have a separate false value and any other value, including (), is true

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The fundamental underlying idea is: all expressions return a value

Lisp knows the value of everything, but the cost of nothing

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The functions car and cdr return parts of lists

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 ${\tt cdr}$ gives us the rest of the list, called ${\tt rest}$ or tail in some Lisps

Note that in (car '((a b) (c d))) the first item in the list is (a b)

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```

```
Exercise. What is (cdr '((a b) (c d)))?
```

Lisp History

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The head was the contents of the address register: car

The tail was the contents of the decrement register: cdr

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- (car '(a b c)) is a
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- (car (cdr (cdr '(a b c)))) is c
- (cdr (cdr '(a b c)))) is ()

car and cdr of () is another dodgy point

```
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```

```
Some Lisps give an error for (car ()) and (cdr ())
```

Some give () as the value for both (efficiency over semantics, again)

car and cdr are primitives: list is not

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You can tell why list is often provided as well as the primitive cons

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A list is really just a pair whose second element is a list

Essentially, if the cdr is a list Lisp prints a space then the cdr (recursively)

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If the cdr is not a list, it prints a dot then the cdr

This produces the nice list output for lists and only prints dots for pairs that are not lists

Exercise. Predict the result of printing

```
• (cons 1 ())
```

```
• (cons (cons 1 2) (cons 3 4))
```

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Exercise. What would this look like when printed?

Lists are supremely suited for recursive procedures

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Most recursions are like

Treat the base case

Lists are supremely suited for recursive procedures

- Treat the base case
- Otherwise do something with some part of the problem

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```
int factorial(int n)
{
  if (n < 2) return 1;
  return n*factorial(n-1);
}</pre>
```

A list is exactly the right structure for this

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• Treat the base case: often ()

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A list can be *defined* recursively

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A list can be defined recursively

A list is

- ()
- or an object (the car)
- consd onto a list (the cdr)

We have

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• (car (cons x 1)) returns x

We have

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To explain the "something like" will take some time

Lists

We have

- (car (cons x 1)) returns x
- (cdr (cons x 1)) returns 1
- (cons (car 1) (cdr 1)) return something like 1

To explain the "something like" will take some time

But before that, we need to see more Lisp basics

Lisp

Basic Lisp Functionality

We now whizz though the basic Lisp bits and pieces: they are from EuLisp, but as always other Lisps are similar, but maybe different

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Constants

- numbers: 1 integer and 1.0 float
- strings: "hello world"
- characters: #\c for the character 'c'
- vectors: #(1 (b c) "hi") a vector of length 3, indexed from 0 to 2

Lists: cons and list, quoted constant '(a b c)

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setter is a general update mechanism

All arguments can be arbitrary expressions, here and elsewhere

Lisp Expressions

Anything that is not constant will be evaluated; things prefixed by quote are constant

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Usually it's the obvious value from the function call

((setter vector-ref) v 3 99) returns 99

Expressions

A special form progn collects together several expressions and wraps them into a single expression

```
(progn
expr1
expr2
...
exprn)
```

This evaluates the exprs sequentially in order and its value is the value of the last exprn

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Exercise. Why is progn a special form?

Expressions

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(progn
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  (+ 2 3))
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prints the message and returns 5

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progn is useful for when Lisp expects a single expression but we want to do more than one thing

The progn wraps several things up and makes a single expression out of them

Expressions

A related special form introduces local variables

The vars are symbols

Its value is the value of the last exprn

Expressions

The vals can be arbitrary expressions; they are evaluated in some order, **then** the vars are given the corresponding values

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The body of the let can use the variables; they revert to whatever they were before (or being undefined) on exit

Expressions

```
(let ((a 1)
          (b (let ((x 2)) (* x x))))
  (foo a b)
    (* a (- b a)))

(let ((car cdr)
          (cdr car))
    (cdr '(a b))) -> a
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Take care with this kind of thing: you can write unreadable code in any language

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Take care with this kind of thing: you can write unreadable code in any language

Exercise. Rewrite the second let for a Lisp-2

Expressions

Exercise. What is the value of

Expressions

There is also a let*

This is like let, but evaluates the vals in the given order, assigning to the vars as it goes; thus val2 can refer to the just-computed value of var1

Expressions

Exercise.

Exercise. Think about how let* could be implemented using let

Expressions

let* is more like the way local variables are declared in other languages

Each variable in the initialiser refers to its closest declaration, be it inside this block or not

let is more general and can be more efficient than let*

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For example, the values in a let might be able to be evaluated in parallel: a let* explicitly denies this

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Case is significant in EuLisp: car and Car are different symbols

Conditionals: if is a simple special form

(if condition expr1 expr2)

Evaluate the condition; if true, evaluate expr1, else evaluate expr2

The value returned from the if is the value of whichever expr that was evaluated

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if plays the role of both if and ?: in C:

$$y = 2*(x > 0 ? 1 : -1) + z$$

Expressions

Expressions

EuLisp also provides

```
(when condition
  expr1
  expr2
  ...
  exprn)
```

Evaluate the condition; if true, evaluate the exprs in order and return the value of the last; otherwise return ()

Expressions

EuLisp also provides

```
(unless condition
  expr1
  expr2
  ...
  exprn)
```

Evaluate the condition; if false, evaluate the exprs in order and return the value of the last; otherwise return ()

Expressions

EuLisp also provides

```
(unless condition
  expr1
  expr2
  ...
  exprn)
```

Evaluate the condition; if false, evaluate the exprs in order and return the value of the last; otherwise return ()

Note: all of if, when and unless are special forms as they treat their arguments specially: in particular, they do not evaluate them unless required

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- (or expr1 expr2 ... exprn) evaluate the exprs in order; whenever any value is true, immediately return it as the value of the or; if all are false, return ()

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- (and expr1 expr2 ... exprn) evaluate the exprs in order; whenever any value is false, immediately return () as the value of the and; if all are false, return the value of the last exprn

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- (and expr1 expr2 ... exprn) evaluate the exprs in order; whenever any value is false, immediately return () as the value of the and; if all are false, return the value of the last exprn

and and or are special forms; not is an ordinary function

Expressions

```
(if (and (> x 0) (not (= y z)))
      (foo x y z)
      (foo y z x))

(foo (or (bar x) (bar y)) 42)
```